

Topics for Projects

Algorithmic Problems Around the Web #1

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CalTech, Fall'07, CS101.2, <http://yury.name/algoweb.html>

Outline

- 1 Administrative Staff / Idea of the Course

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- 2 Challenges in Web Technologies

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- 3 Existing Theory: Nearest Neighbors
- 4 List of Project Topics

Part I

Administrative Staff

Idea of the Course

About Instructor

- Web: <http://yury.name>
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- Cell phone: 1.626.463.3668
- Office: Moore 311, 1.626.395.3863
- Facebook: search “Yury Lifshits”
- Special page: <http://simsearch.yury.name>

Registration Policy

You can

- Join at any time
- Leave at any time
- Attend “just for fun”

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Give me your [name](#), [email](#) and current [status](#) if you want to be informed about all course-related events

Grading Policy (Updated)

- 20% Problem Setting / Literature Review
Short seminar talk at the end
- 40% Work on Project
- 40% Results Presentation
Seminar talk at the end

Feedback / Promotion

- Please report me my mistakes
Slides, English, etc. . .
- Any ideas how to improve the course?
- Is the time slot MW 11-12 ok? Any better option?
- Tell your friends about this course
- Give me a hyperlink

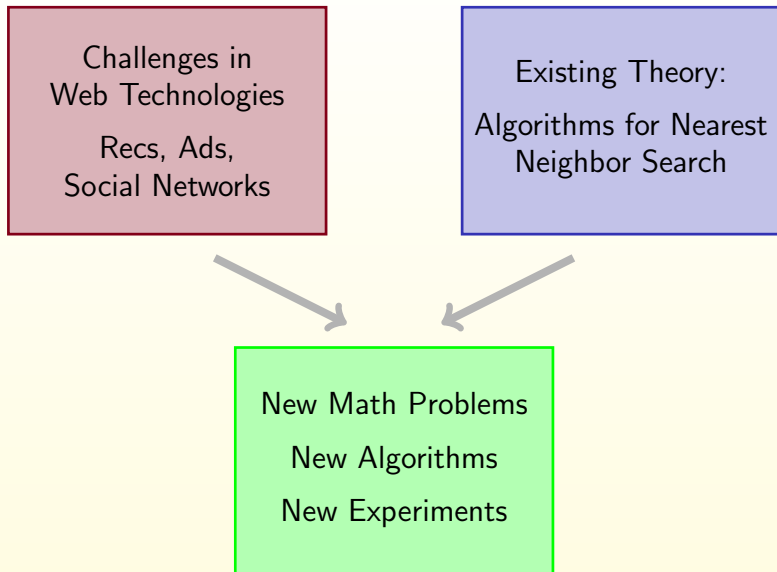
Course Philosophy

Challenges in
Web Technologies

Recs, Ads,
Social Networks

Existing Theory:
Algorithms for Nearest
Neighbor Search

Course Philosophy



Course Schedule

- 5 more lectures
- 12-14 class hours for seminars
- weekly team meetings

Part II

Challenges in Web Technologies

Recommendation Systems

Recommendation systems attempts to present information items (movies, music, books, news, web pages) that are likely of interest to the user

System compares the user's profile to some reference characteristics. These characteristics may be from the information item (the content-based approach) or the user's social environment (the collaborative filtering approach)

Behavioral Targeting

Ad targeting:

Ancient: broadcasting

Current: contextual

Future: behavioral

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The idea is to observe a users online behavior anonymously and then serve the most relevant advertisement based on their behavior

Personalized News Aggregation

A feed aggregator is a Web application which aggregates syndicated web content such as news headlines, blogs, podcasts, and vlogs in a single location for easy viewing

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Challenge: personalized aggregation

Social Networks Analysis

Social network:

Nodes

Edges

Examples of relations: financial exchange, friends, dislike, conflict, trade, web links, sexual relations, disease transmission, airline routes, etc.

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Our focus

Community discovery

Burst detection

Part III
Theory of
Nearest Neighbors

Nearest Neighbors Informally

To preprocess a database of n objects so that given a query object, one can effectively determine its nearest neighbors in database

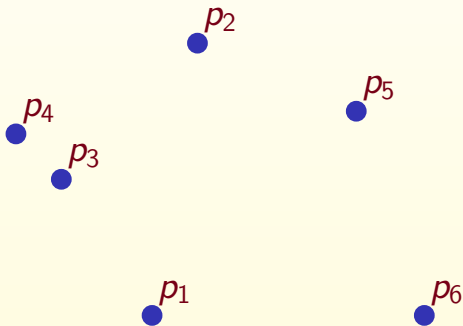
More Formally

Search space: object domain \mathbb{U} , similarity function σ

Input: database $S = \{p_1, \dots, p_n\} \subseteq \mathbb{U}$

Query: $q \in \mathbb{U}$

Task: find $\operatorname{argmax}_{p_i} \sigma(p_i, q)$



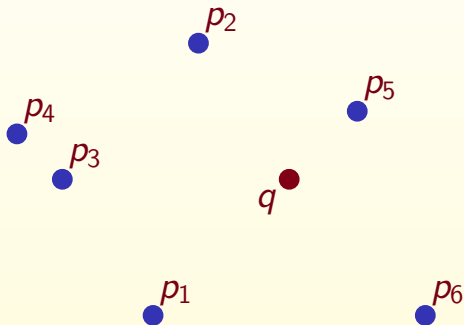
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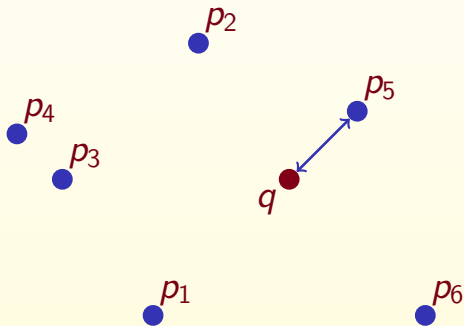
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Some Solutions for NN Problem

Sphere Rectangle Tree Orchard's Algorithm LAESA

k-d-B tree Geometric near-neighbor access tree

Excluded middle vantage point forest mvp-tree Fixed-height

fixed-queries tree AESA **Vantage-point tree**

R*-tree Burkhard-Keller tree BBD tree

Navigating Nets Voronoi tree Balanced aspect ratio tree Metric tree

vp^s-tree **M-tree** Locality-Sensitive Hashing

SS-tree **R-tree** Spatial approximation tree Multi-vantage

point tree Bisector tree mb-tree

Generalized hyperplane tree

Hybrid tree Slim tree Spill Tree Fixed queries tree X-tree k-d

tree Balltree **Quadtree** **Octree** Post-office tree

Part IV

List of Project Topics

5 Theoretical / 4 Experimental

T1 Nearest Neighbors for Sparse Vectors

Database: n vectors in \mathbb{R}^m each having at most $k \ll m$ nonzero coordinates

Query: vector in \mathbb{R}^m also having at most $k \ll m$ nonzero coordinates

Similarity: scalar product

T1 Nearest Neighbors for Sparse Vectors

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Is there an algorithm for solving nearest neighbors on sparse vectors within following constraints:
 $poly(n, m)$ preprocessing, $poly(k, \log n, \log m)$ query?

T2 LD Embeddings for Social Networks

Input:

Friendship graph / Co-authorship graph

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How to construct embedding into 2D (Euclidean plane)
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Workflow:

Define social network model

Define distortion of 2D embedding

Find embedding algorithm with least possible distortion

T3 Disorder Method for Nearest Neighbors

Sort all objects in database S by their similarity to p
Let $\text{rank}_p(s)$ be position of object s in this list

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Disorder inequality for some constant D :

$$\forall p, r, s \in \{q\} \cup S : \quad \text{rank}_r(s) \leq D \cdot (\text{rank}_p(r) + \text{rank}_p(s))$$

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What is the most efficient algorithm for nearest neighbor search in terms of n and D ?

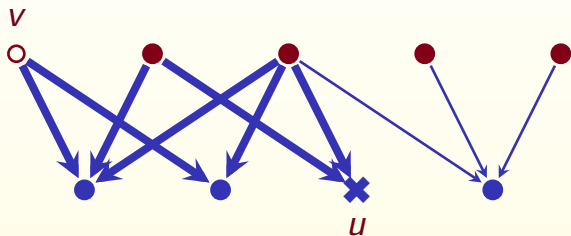
T4 3-Step Nearest Neighbors

3-step similarity between boy and girl in some bipartite boys-girls graph is equal to number of paths of length 3 between them

n boys

boy degrees $\leq k$

m girls



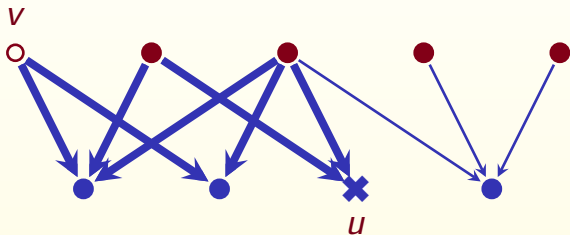
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Construct an algorithm for solving nearest neighbors in bipartite graphs with 3-step similarity

Constraints: $poly(n, m)$ preprocessing, $poly(k, \log n, \log m)$ query

T5 Probabilistic Nearest Neighbors

Probabilistic Analysis in a Nutshell

- Define a probability distribution over databases
- Define probability distribution over query objects
- Construct a solution that is efficient/accurate with high probability over “random” input/query

E1 Recommendations for Blog Posts

Available information:

Friendship graph

Comments, hyperlinks

Keywords of interests, post content

Task: For every user recommend 10 posts from last day that seems to be the most interesting for him/her

E2 CTR Prediction

Available information:

Click-or-not bipartite graph

Task: Predict click-through rate for given pair “user-ad”

E3 Social Networks Visualization

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Tasks:

- Compute disorder values for various datasets
- Implement disorder-based algorithms for NNS
- Study their performance

ToDo List

- Choose a project, form a team
- Make a quick look at corresponding references
- Schedule a meeting with me on this week

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- Recommend this course to friends

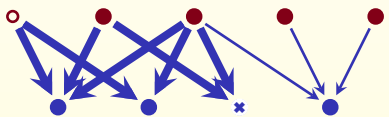
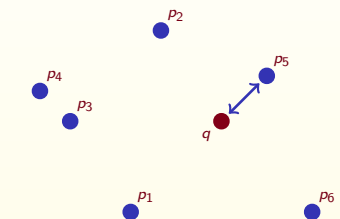
Last Slide

Challenges in
Web Technologies

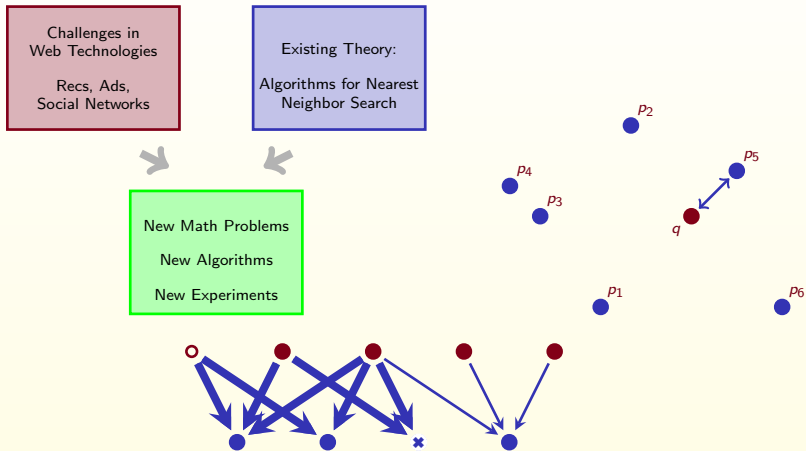
Recs, Ads,
Social Networks

Existing Theory:
Algorithms for Nearest
Neighbor Search

New Math Problems
New Algorithms
New Experiments



Last Slide



Thanks for your attention! Questions?